



# Number Systems

## Decimal # System

$10^3$	$10^2$	$10^1$	$10^0$
1,000s	100s	10s	1's
0	4	6	2

Each digit is 10 characters <sup>one-of</sup>  
0-9

Base 10

$$= 0 \times 1000 + 4 \times 100 + 6 \times 10 + 2 \times 1$$

## Binary # System

→ Base 2

Each digit: 0 or 1  
False True

128 64 32 16 8 4 2 1

$2^7$   $2^6$   $2^5$   $2^4$   $2^3$   $2^2$   $2^1$   $2^0$

0b 0 1 0 0 1 1 0 1

↑  
identifies  
as binary  
#

$$= 0 \times 128 + 1 \times 64 + 0 \times 32 \dots + 1 \times 8 + 4 + 1 = 77$$

↑ Binary to Decimal Conversion.

Decimal  $\rightarrow$  Binary  
Dec  $\rightarrow$  Bin

$$\begin{array}{r} 77 \\ -64 \\ \hline 13 \\ -8 \\ \hline 5 \\ -4 \\ \hline 1 \\ -1 \\ \hline 0 \end{array}$$

	128	64	32	16	8	4	2	1
	<del>2<sup>7</sup></del>	2 <sup>6</sup>	2 <sup>5</sup>	2 <sup>4</sup>	2 <sup>3</sup>	2 <sup>2</sup>	2 <sup>1</sup>	2 <sup>0</sup>
...	0	0	1	0	0	1	1	0
								1

Method 1: See if it fits

We'll see this (kind of) later  
in the semester. --

Dec  $\rightarrow$  Bin Conversion

Method 2: Divide-By-The-Base

$$\begin{array}{r} 77 \\ \div 2 \\ \hline 38 \text{ R } 1 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 19 \text{ R } 0 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 9 \text{ R } 1 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 4 \text{ R } 1 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 2 \text{ R } 0 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 1 \text{ R } 0 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 0 \text{ R } 1 \end{array}$$

$$\begin{array}{r} 12 \\ \div 2 \\ \hline 0 \text{ R } 0 \end{array}$$

0 1 0 0 1 1 0 1

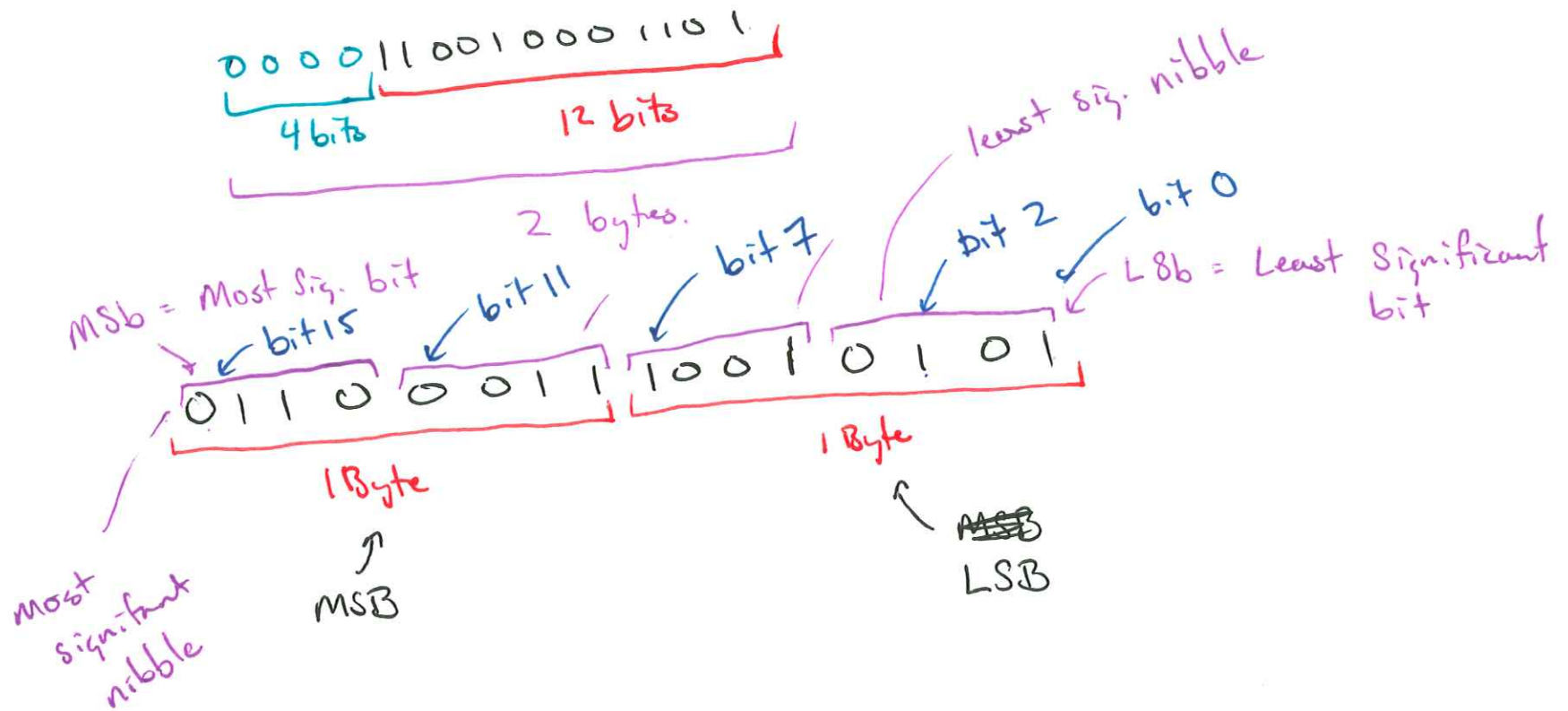


# Binary Terminology

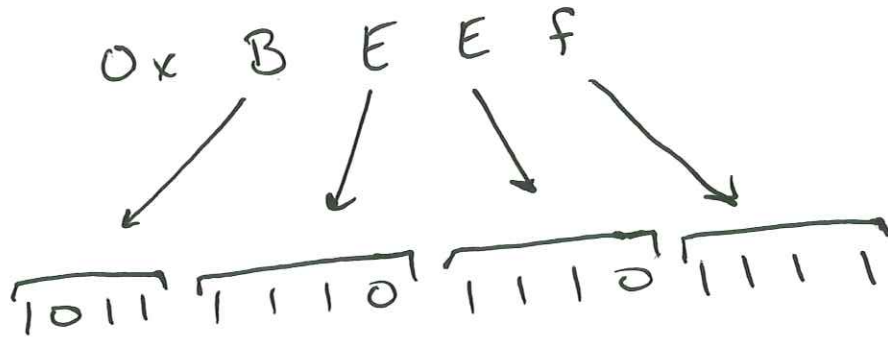
1 Binary Digit = 1 Bit.

8 Bits = 1 Byte

whenever we represent Binary data in this class do so using full bytes. for ex:



Hex  $\rightarrow$  Bin:



	Dec	Hex
0000	= 0	= 0
0001	= 1	= 1
...		
1110	= 14	= E
1111	= 15	= F

0b 010010001101001110100110

4 8 D 3 A 6

$\hookrightarrow$  0x 48D3A6  $\rightarrow$  3 bytes, 6 nibbles, 24 bits.

Ex Change above # Bit 19 to 1

Digit 8 must have bits 19-16  
 $\downarrow$  19 18 17 bit 16  
1 0 0 0