ENGR-4300
Electronic Instrumentation
Quiz 2
Fall 2011
Name $\qquad$

## Section

$\qquad$

Question I (20 points) $\qquad$
Question II (20 points) $\qquad$
Question III (20 points) $\qquad$
Question IV (20 points) $\qquad$
Question V (20 points) $\qquad$

Total (100 points) $\qquad$
On all questions: SHOW ALL WORK. BEGIN WITH FORMULAS, THEN SUBSTITUTE VALUES AND UNITS. No credit will be given for numbers that appear without justification.

## Question I - Bridges and Damped Sinusoids (20 points)

You are given a cantilever beam similar to the one you used in experiment 4. You place two weights on the end of the beam one at a time $(0.138 \mathrm{~kg}$ and 0.86 kg$)$ and you get the following two plots (may not be in order of mass listed).


Plot 2


## Question I - Bridges and Damped Sinusoids (continued)

1) (2pt) What is the frequency of plot 1 ? (Use at least 2 significant figures)

9 cycles in 1 second $=9.0 \mathrm{~Hz}$
2) (2pt) What is the frequency of plot 2 ? (Use at least 3 significant figures)

4 cycles in 1 second $=4.00 \mathrm{~Hz}$
3) (6pt) What is the damping constant for plot 1 , mark the points on the plot? (Use at least 3 significant figures)

The signal amplitude drops to 0.4 from 1 in 1 second. $e^{-\alpha 1}=0.4$ so that $-\alpha=\log 0.4=-0.916$ where the two points are indicated with the arrows.

The actual number used in the Matlab program that generates the curves was 0.9
4) $(6 \mathrm{pt})$ Given the following formula, $k=\left(m+m_{n}\right)\left(2 \pi f_{n}\right)^{2}$, and assuming that the two data points that you found are ideal, find values for k and m .
$k=\left(m+m_{n}\right)\left(2 \pi f_{n}\right)^{2} k=(m+0.138)(2 \pi 9)^{2} k=(m+0.86)(2 \pi 4)^{2}$
gives us $k=570, m=0.04$

## Question I - Bridges and Damped Sinusoids (continued)

5) $(2 \mathrm{pt})$ What is the mass of the beam?
$m_{b}=\frac{0.04}{0.23}=0.174 \mathrm{~kg}$
6) (2pt) Using the chart for Young's Modulus, determine the probable material that the beam is made out of given that the dimensions of the beam are: width $=1.5 \mathrm{~cm}$, length= 15 cm , and thickness $=2 \mathrm{~mm}$.

| TABLE 9.1 |  |  |  |
| :---: | :---: | :---: | :---: |
| Young's Modulus Table of Values |  |  |  |
| Metal | Elastic modulus ( $\mathrm{N} / \mathrm{m} 2$ ) | Metal | Elastic modulus ( $\mathrm{N} / \mathrm{m} 2$ ) |
| aluminum, $99.3 \%$, rolled | $6.96 \times 10^{10}$ | lead, rolled | $1.57 \times 10^{10}$ |
| brass | $9.02 \times 10^{10}$ | platinum, pure, drawn | $16.7 \times 10^{10}$ |
| copper, wire, hard drawn | $11.6 \times 10^{10}$ | silver, hard drawn | $7.75 \times 10^{10}$ |
| gold, pure, hard drawn | $7.85 \times 10^{10}$ | steel, $0.38 \% \mathrm{C}$, annealed | $20.0 \times 10^{10}$ |
| iron, wrought | $19.3 \times 10^{10}$ | tungsten, drawn | $35.5 \times 10^{10}$ |

$k=570 \quad w=1.5 \mathrm{~cm} \quad l=15 \mathrm{~cm} \quad t=2 \mathrm{~mm} \quad E=\frac{k 4 l^{3}}{w t^{3}}=6.44 \times 10^{10} \frac{\mathrm{~N}}{\mathrm{~m}^{2}}$ aluminum

## Question II - Thevenin Equivalents (20 points)



1) (7pt) Find the Thevenin equivalent voltage with respect to A and B for the circuit shown above)

For $V_{\text {th }}$ there is no load (open circuit) so that there is no voltage drop across R4. To find the voltage from $A$ to $B$, first find the voltages at points $1-3$. Combine $R 3+R 7=2 k$. Then $R 6 \|(R 3+R 7)=1 k$. Then $R 2+R 6 \|(R 3+R 7)=2 k$ and finally $R 5 \|(R 2+R 6 \|(R 3+R 7))=1 k$. Thus, $V_{1}=8, V_{2}=4, V_{3}=2$ are obtained from voltage divider formulas.

From PSpice

2) ( 6 pt ) Find the Thevenin equivalent resistance with respect to $A$ and $B$ for the circuit shown above.

Short out the voltage source. Then $R_{t h}=1 k+1 k\|(1 k+2 k \|(1 k+2 k \| 2 k))=1 k+1 k\| 2 k=1.67 k$

## Question II - Thevenin Equivalents (continued)

3) (5pt) Draw the Thevenin equivalent circuit with a load resistor RL of 5 K between points A and B

4) (2pt) What is the voltage across $\mathrm{R}_{\mathrm{L}}$ ?

The voltage is $2(5 / 6.667)=1.5$

## Question III - Op-Amp Applications (20 points)



Assume the following components in the above circuit:
$\mathrm{V} 1: \mathrm{V}_{\text {off }}=200 \mathrm{mV}, \mathrm{V}_{\text {ampl }}=200 \mathrm{mV}, \mathrm{f}=1 \mathrm{kHz} ; \mathrm{V} 2: \mathrm{V}_{\text {off }}=0 \mathrm{~V}, \mathrm{~V}_{\text {ampl }}=200 \mathrm{mV}, \mathrm{f}=1 \mathrm{kHz}$
$\mathrm{R} 1=\mathrm{R} 2=1 \mathrm{k} \Omega, \mathrm{R} 3=\mathrm{R} 4=10 \mathrm{k} \Omega, \mathrm{R} 5=1 \mathrm{M} \Omega$

1) (1pt) The circuit above is an amplifier you've seen. What type of amplifier is it?

## Differential Amp

2) (3pt) Write the general equation for the output $C(V c)$ in terms of the input voltages $V 2$ and V1. Simplify (Do not enter specific voltage values but use the values of the resistors)
$V_{C}=V_{2} \frac{R 4}{R 2}-V_{1} \frac{R 3}{R 1}=10\left(V_{2}-V_{1}\right)$

## Question III - Op-Amp Applications (continued)

3) (16pt) Sketch and label one cycle of the input at V2 (point B), the input at V1 (point A) and the output at $\mathrm{C}(\mathrm{Vc})$ on the plot below



## Question IV - Op-Amp Integrators and Differentiators (20 points)



1) (2pt) What function is this ideal circuit designed to perform?

## Differentiator

2) ( 2 pt ) Write the general, frequency dependent transfer function $V_{\text {out }} / V_{\text {in }}$ for this circuit. Then substitute in the values $\mathrm{R}=1 \mathrm{k} \Omega$ and $\mathrm{C}=0.4 \mu \mathrm{~F}$. Then write the expression for $\mathrm{V}_{\text {out }}(\mathrm{t})$ in terms of $\mathrm{V}_{\text {in }}(\mathrm{t})$ as a function of time. Hint: use the formula sheet.
$\frac{V_{\text {out }}}{V_{\text {in }}}=-j \omega R C=-j \omega(0.0004) \quad V_{\text {out }}=-R C \frac{d V_{\text {in }}}{d t}=-0.0004 \frac{d V_{\text {in }}}{d t}$
3) (4pt) Based on the transfer function in time, determine the output voltage for the input shown below. Plot the output. Slope is $2 /(5 \mathrm{~ms})=400$. $R$ C times the derivative is 0.16


Up to this point, this question has addressed the ideal op-amp configuration. The usual next step in the investigation process is to do a PSpice simulation. The circuit and the simulation results are shown below.



20 ms
It is possible to achieve results much more like those predicted by the ideal model if we add a capacitor $\mathrm{C} 2=0.015 \mu \mathrm{~F}$ in parallel with the $1 \mathrm{k} \Omega$ feedback resistor. The remaining questions relate to the modified circuit.
4) (4pt) Write the general, frequency dependent transfer function $V_{\text {out }} / V_{\text {in }}$ for this circuit.
$\frac{V_{\text {out }}}{V_{\text {in }}}=-\frac{R \| C 2}{1 / j \omega C}=-\frac{\left(\frac{R}{1+j \omega R C 2}\right)}{1 / j \omega C}=-\frac{j \omega R C}{1+j \omega R C 2}$
5) (3pt) Find the corner frequency $f_{c}$ for the circuit in Hz .

The corner frequency is where $\omega R C 2=1$ or $f_{c}=\frac{1}{2 \pi R C 2}=\frac{1}{2 \pi 10^{3} 4\left(10^{-7}\right)}=397 \mathrm{~Hz}$
6) (3pt) For which frequencies will the circuit perform the desired function? Explain.
a. Low frequencies below $\omega_{c}$
b. Only a mid band of frequencies around $\omega_{c}$
c. High frequencies above $\omega_{c}$
7) (2pt) Based on your answer to the previous question, simplify the transfer function for frequencies where the circuit performs the desired function. That is, simplify for low frequencies, high frequencies or frequencies near $\omega_{c}$.
$\frac{V_{\text {out }}}{V_{\text {in }}}=-\frac{j \omega R C}{1+j \omega R C 2}=-j \omega R C$ because the second term in the denominator is small enough to be neglected.

## Question V - Troubleshooting, Debugging (20 points)

Which of the following have been discovered while troubleshooting/debugging experimental and simulated circuits for some group in this class ( 1 pt each)?

1. $680 \mathrm{k} \Omega$ resistors used instead of $680 \Omega$ resistors.
2. Connections to +4 V and -4 V reversed.
3. Large DC offset in signal not observed because the oscilloscope was set up for AC coupling rather than DC coupling.
4. Transistor or integrated circuit plugged in backwards.
5. No power to integrated circuit.

Identify and the following circuit components:
6. Component number one ( 3 pts ).

Also give its value.
Capacitor. Value is 47 times $10^{4} \mathrm{pF}$ or $0.47 \mu F$

7. Component number two ( 3 pts ).

Also give its value.
Potentiometer. Value is 50 time $10^{4}$ or $500 \mathrm{k} \Omega$

8. Component number three (3 pts).

## Transistor


9. Power Supplies (3pts) Circle all correct answers.


For a 9V battery connector (shown above) and the PSpice circuit diagram (above right)

$\bigcirc$Wire A represents the red wire and Wire B represents the black wire
Wire B represents the red wire and Wire A represents the black wire

- Wire A is connected to the circuit ground to provide +9 V at some other point in a circuit Wire B is connected to the circuit ground to provide +9 V at some other point in a circuit Wire A is connected to the circuit ground to provide -9 V at some other point in a circuit Wire B is connected to the circuit ground to provide -9 V at some other point in a circuit

10. 741 Op-Amp (3pts) Circle all correct answers.

Shown below is a photo of a 741 op-amp. The small dimple is at the left.


- The pins on the op-amp are numbered as shown in the figure labeled A
- The pins on the op-amp are numbered as shown in the figure labeled $B$

The 741 requires a positive DC voltage (e.g. +9 V ) on pin 4 and a negative DC voltage (e.g. -9 V ) on pin 7 to operate

- The 741 requires a negative DC voltage (e.g. -9V) on pin 4 and a positive DC voltage (e.g. +9 V ) on pin 7 to operate
- The output signal is found on pin 6

The output signal is found on pin 2

- The output signal is found on pin 3
- The input signal is connected to either pin 2 or pin 3

