ENGR-2300
Electronic Instrumentation
Quiz 1
Spring 2023

## Print Name

$\qquad$ RIN

## Section

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I have read, understood, and abided by the Collaboration and Academic Dishonesty statement in the course syllabus. The work presented here was solely performed by me.

Signature: $\qquad$

## Date:

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On all questions: SHOW ALL WORK. BEGIN WITH FORMULAS, THEN SUBSTITUTE VALUES AND UNITS. No credit will be given for numbers that appear without justification. Unless otherwise stated in a problem, provide 3 significant digits in answers. Read the entire quiz before answering any questions. Also, it may be easier to answer parts of questions out of order.

## I. Circuit Analysis (16 points)

DC Voltage Divider Questions
The following circuit has three voltage sources:


1. ( 3 pts ) Find Vout given the resistances $\mathrm{R} 1=10 \mathrm{~K}, \mathrm{R} 2=5 \mathrm{~K}$, and $\mathrm{R} 3=20 \mathrm{~K}$ ohms.
2. (2 pts) Find the current through R1, R2, R3 and RL.
3. ( 4 pts ) The following circuit has a voltage dividing function. Derive the transfer function equation (Vout/Vin) in terms of V1, C1, C2 and C3. (Hint: even though Vin is a DC source, still approach this question using the concept of the impedance of a capacitor.)

4. (1 pts) What is the value of Vout for the case of $\mathrm{V} 1=12 \mathrm{~V}, \mathrm{C} 1=5 \mathrm{uF}, \mathrm{C} 2=2 \mathrm{uF}$ and $\mathrm{C} 3=7 \mathrm{uF}$ ?

The following circuit has a 12 V DC voltage source connected to a resistor ( 1 k ohm ) and an inductor $(1 \mathrm{mH})$. It has been switched ON for a while and switches OFF at $\mathrm{t}=0$.

5. (3 pts) What is the current through R1 ( 1 K ohm) before the circuit switches OFF?
6. (3 pts) At $=0$, the circuit is switched OFF, and it takes 10 us to settle down to zero current. What is VL (voltage across the inductor)?

## II. Filters (24 points)

RC Circuit Questions


1. (2 pts) V1 is an AC source with varying frequency ( $\omega$ ). Find the transfer function (Vout/Vin) in terms of $\omega, \mathrm{R} 1$ and C 1 .
2. (1 pt) What is the simplified transfer function equation at two extreme frequencies (low: $\omega \rightarrow 0$, and high: $\omega \rightarrow \infty$ )?
3. (1 pt) Find the corner frequency of this RC circuit for the case: $\mathrm{R} 1=100 \mathrm{ohm}, \mathrm{C} 1=0.1 \mathrm{uF}$.
4. ( 1 pt ) Is this a high pass or low pass filter?

You must include units.

## RL Circuit Questions



1. (2 pts) V1 input is AC with varying frequency $(\omega)$. Find the transfer function (Vout/Vin) in terms of $\omega$, R1 and L1.
2. (1 pt) What is the simplified transfer function equation at two extreme frequencies (low: $\omega \rightarrow 0$, and high: $\omega \rightarrow \infty$ ).
3. (2 pts) Find the corner frequency of this RL circuit for the case: $\mathrm{R} 1=100 \mathrm{ohm}, \mathrm{L} 1=0.4 \mathrm{H}$.
4. (1 pt) Is this a high pass or low pass filter?

## RLC Circuit Questions

Now we want to build a new filter by cascading the filters above.


## Cascade two filters into one by sharing Vin source \& R1



1. (4 pts) V1 input is the same: AC with varying frequency $(\omega)$. Find the transfer function (Vout/Vin) of the new filter in terms of $\omega$, R1, C1, and L1.
2. (1 pt) What is the simplified transfer function equation at two extreme frequencies (low: $\omega \rightarrow 0$, and high: $\omega \rightarrow \infty$ ).
3. (1 pt) Draw simplified circuit diagrams for the two extreme cases (low: $\omega \rightarrow 0$, and high: $\omega \rightarrow \infty$ ).
4. (2 pts) Derive the equation for the resonant frequency of this filter. Show your reasoning and assumptions in derivation process. (Hint: at what $\omega$ does the magnitude of the transfer function have a maximum? $\left|\mathrm{H}_{\max }\right|=1$ )
5. (2 pts) What is the phase angle of the transfer function at the resonant frequency? Show the calculation process.
6. (1 pt) Now we have two corner frequencies. If the values of $R, C$ and $L$ have the same values as in previous questions ( $\mathrm{R} 1=100 \mathrm{ohm}, \mathrm{L} 1=0.4 \mathrm{H}$ and $\mathrm{C} 1=0.1 \mathrm{uF}$ ), what kind of filter is this?
a. Low pass filter
b. High pass filter
c. Band pass filter
d. Band reject filter
7. (2 pts) Draw the transfer function in a linear plot, specifying the two corner frequencies on the $x$ axis (frequency axis). A rough drawing is $\mathrm{OK}: \mathrm{H}(\omega)$ max is 1 on the y -axis. Labeling of the corner frequency and the relative amplitude on a linear scale on the $y$-axis is important.


You must include units.
11

## III. Inductors, Transformers, and Phasors (20 points)

## Inductors and Transformers

You are given a transformer connected to a source and load circuit, as shown below. You know nothing about the transformer except that the wire is wound around a ferrite core.


1. (4 pts) With an AC voltage applied to the circuit, you measure $\mathrm{VS}=4 \mathrm{~V}$ and $\mathrm{IS}=320 \mathrm{~mA}$. If $Z_{i n}=\frac{V S}{I S}$, what is the value of $a$ ?
2. ( 2 pts ) If you remove RL such that the load is now an open circuit, no current will flow through the load circuit and no voltage will form across the load side's inductor. In this case you can measure the impedance of LS, the inductor on the source side.

At a frequency of $f=10 \mathrm{kHz}$, you measure the impedance of the source side's inductor to be $\mathrm{Z}_{\mathrm{LS}}=\mathrm{j} 188.5 \Omega$. What is the inductance LS?
3. (3 pts) If the toroidal, ferrite core has an inductance factor of $L_{f}=10.6 \mu \mathrm{H} / \mathrm{turns}^{2}$, how many wire turns are in inductor LS (round up to the nearest whole number)?
4. ( 2 pts ) How many wire turns are in inductor LL (round up to the nearest whole number)?
5. (3 pts) How much current is flowing through RL, given $\mathrm{VS}=4 \mathrm{~V}$ as in question 1 ?
6. ( 2 pts ) True or false: for every transformer, there exists a minimum frequency below which the transformer will not behave as the equations predict.

## Phasors

7. (4 pts) If you combine the impedances in circuit A below into an effective impedance Zeff, as shown in circuit B, what is the magnitude of Zeff?


## IV. Instrumentation Fundamentals and Concepts ( 20 points)

1. ( 6 pts ) In experiment 3 , you estimated the inductance of your homemade inductor by measuring the resonant frequency of a circuit similar to the one below. By drawing lines from the channels to locations in the circuit, show how you would:
a. Source the voltage Vin from the instrumentation board
b. Measure the input voltage (Vin)
c. Measure the output voltage (Vout)

2. (2 pts) If you measured an oscillation frequency of $f_{0}=5 \mathrm{kHz}$, what would be your estimate for the inductance of inductor L 1 (to the nearest 0.01 mH )?
3. (2 pts) If the non-idealities of the instrumentation board are considered, the input impedance of the board must also be modeled, resulting in the following circuit.


In this case, the value of the input resistance is $\mathrm{R} 2=1 \mathrm{M} \Omega$ and the input capacitance is $\mathrm{C} 2=24 \mathrm{pF}$. If you needed to find these values specifically for the M2K or the Analog Discovery 2 yourself, where would you find them?
4. (2 pts) To determine the effect of the input capacitance on your inductance estimate, combine C 1 and C2 in the circuit in IV. 3 into a single, effective capacitance and recalculate L1 using the same resonant frequency as in IV. 2 (to the nearest 0.01 mH ).
5. ( 2 pts ) Given that C 2 is fixed at 24 pF for a given instrumentation board, under what circumstances for C 1 would you need to be concerned that the input capacitance of the board is significantly affecting your measurement?

## Miscellaneous Concepts

6. (2 pts) Suppose that you calculate that the output voltage from a circuit should be $V_{\text {out }}=500(1+j) \mathrm{mV}$. What is the amplitude of the voltage that you expect to measure?
7. ( 1 pt ) Why doesn't it matter where the two inductor coils of a transformer are located on a ferrite core, as opposed to an air core?
8. (1 pt) Circle one: you run an AC sweep of the circuit to the right and determine that the circuit acts as a high-pass filter when you measure the voltage across Z2 (Vout2). What kind of filter would you have if you instead measured across Z1 (Vout1)?
a) high-pass filter
b) low-pass filter
c) band-pass filter
d) band-reject filter

e) Not enough information to determine the type of filter

You must include units.
9. (1 pt) Describe how you would measure the current flowing through a resistor using the M2K or Analog Discovery 2.
10. (1 pt) Circle one: what effect would replacing the ferrite core of an inductor with an air core have on the inductance of that inductor?
a) decrease the inductance
b) leave the inductance unchanged
c) increase the inductance
d) the inductance would be zero

