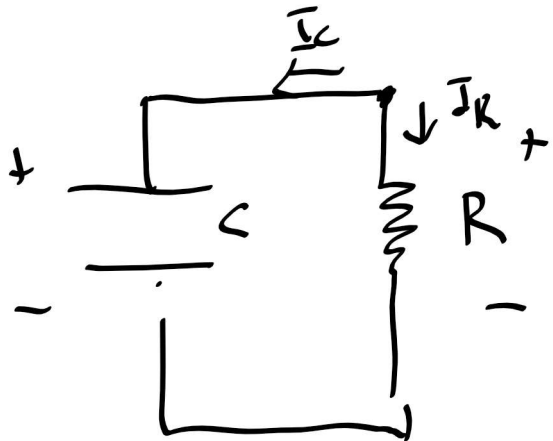


RC:  $\dot{V}_C = \frac{dV_C}{dt}$

$$I_C + I_R = 0$$



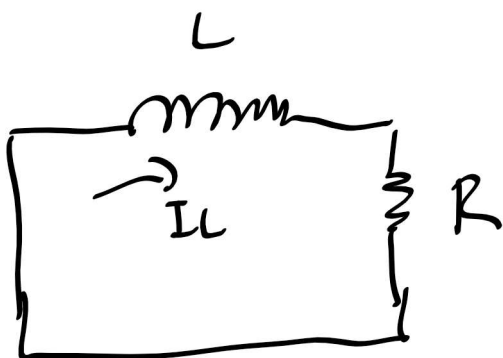
$$C\dot{V}_C + \frac{V_R}{R} = 0$$

$$C\dot{V}_C + \frac{V_C}{R} = 0$$

$$\dot{V}_C = -\frac{1}{RC} V_C$$

$$V_C(t) = V_0 e^{-t/RC}$$

RL:



$$\dot{I}_L = -\frac{R}{L} I_L$$

$$I_L(t) = I_0 e^{-\frac{R}{L}t}$$

$$\dot{V}_C = -\frac{1}{RC} V_C \quad \leftarrow$$

$$V_C(t) = V_0 e^{-t/RC}$$

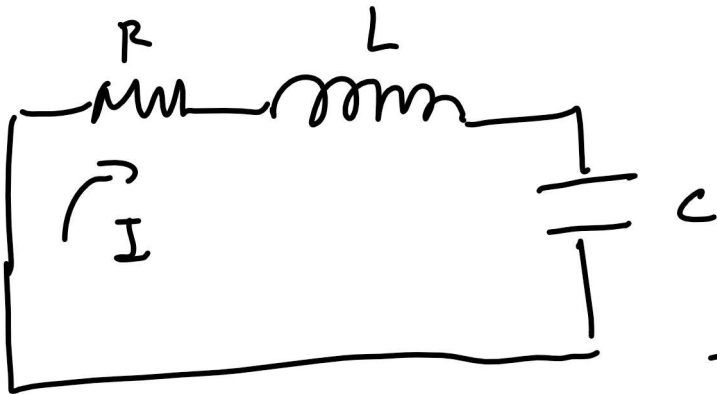
$$\dot{V}_C(t) = \frac{d V_C(t)}{dt} = -\frac{1}{RC} \underbrace{V_0 e^{-t/RC}}_{V(t)}$$

$$\dot{V}_C(t) = -\frac{1}{RC} V(t) \quad \leftarrow$$

RLC:

$$V_R + V_L + V_C = 0$$

$$RI + L \dot{I} + V_C = 0$$



$$\rightarrow I = C \dot{V}_C = C \frac{dV_C}{dt}$$

$$RC \frac{dV_C}{dt} + LC \frac{d^2 V_C}{dt^2} + V_C = 0$$

$$\frac{d^2 V_C}{dt^2} = -\frac{1}{LC} V_C - \frac{R}{L} \frac{dV_C}{dt}$$

$$X = \begin{bmatrix} V_C \\ \frac{dV_C}{dt} \end{bmatrix}$$

$$\frac{dX}{dt} = \begin{bmatrix} \frac{dV_C}{dt} \\ \frac{d^2 V_C}{dt^2} \end{bmatrix} = \begin{bmatrix} \frac{dV_C}{dt} \\ -\frac{1}{LC} V_C - \frac{R}{L} \frac{dV_C}{dt} \end{bmatrix}$$

$$X = \begin{bmatrix} v_c \\ \frac{dv_c}{dt} \end{bmatrix}$$

$$\frac{dX}{dt} = \begin{bmatrix} \frac{dv_c}{dt} \\ \frac{d^2v_c}{dt^2} \end{bmatrix} = \begin{bmatrix} \frac{dv_c}{dt} \\ -\frac{1}{LC} v_c - \frac{R}{L} \frac{dv_c}{dt} \end{bmatrix}$$

$$\frac{dX}{dt} = \underbrace{\begin{bmatrix} 0 & 1 \\ -\frac{1}{LC} & -\frac{R}{L} \end{bmatrix}}_A \begin{bmatrix} v_c \\ \frac{dv_c}{dt} \end{bmatrix}_X$$

$$\frac{dX}{dt} = AX$$

$$X(t) = e^{At} x_0$$

$$A = V \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} V^{-1} \quad e^{At} = V \begin{bmatrix} e^{\lambda_1 t} & 0 \\ 0 & e^{\lambda_2 t} \end{bmatrix} V^{-1}$$

$$A = \begin{bmatrix} 0 & 1 \\ -\frac{1}{LC} & -\frac{R}{L} \end{bmatrix}$$

$$\det(A - \lambda I) = \det \begin{bmatrix} -\lambda & 1 \\ -\frac{1}{LC} & -\frac{R}{L} - \lambda \end{bmatrix}$$

$$= -\lambda \left( -\frac{R}{L} - \lambda \right) + \frac{1}{LC}$$

$$= \lambda^2 + \frac{R}{L}\lambda + \frac{1}{LC} = 0$$