

# Class 3: Voltage Dividers

Activity 3 – Voltage Dividers

January 20<sup>th</sup>, 2022

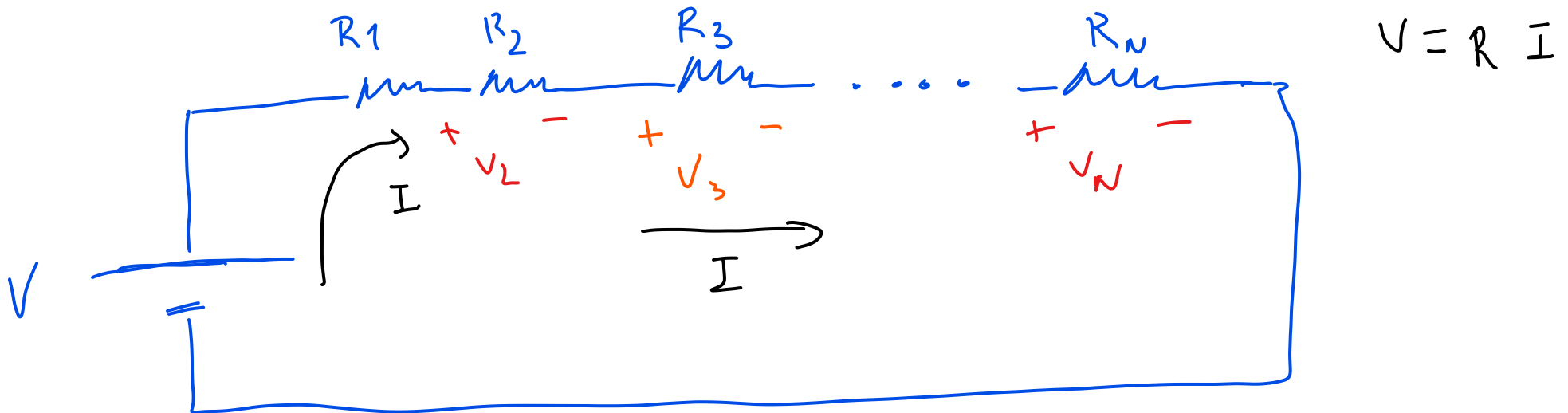
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Intro to ECSE

# Derivation of Voltage Divider Equation

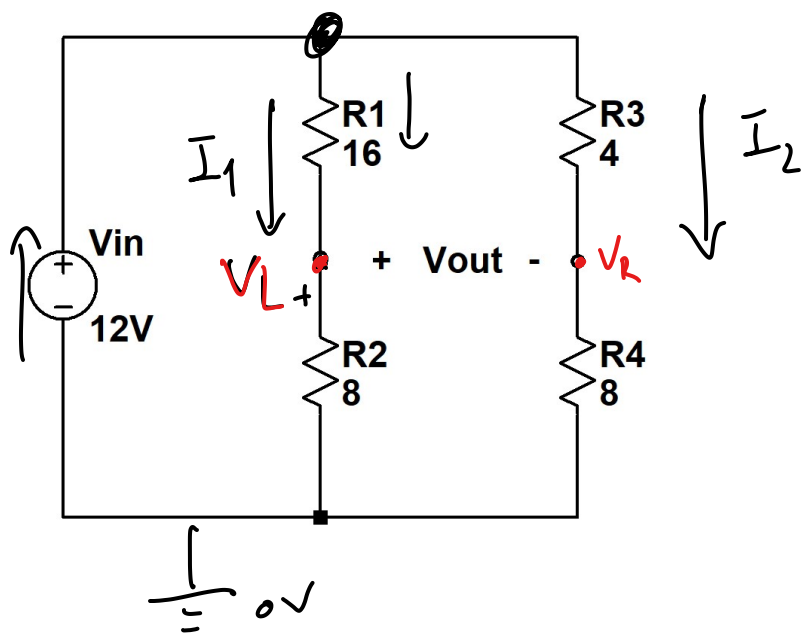


$$I = \frac{V}{R} = \frac{V}{\sum_{k=1}^N R_k}$$

$$V_k = R_k \cdot I = V \cdot \frac{R_k}{\sum_{k=1}^N R_k}$$

↑  
ohm's law

## Example: Find $V_{out}$



$$V_{out} = V_L - V_R$$

$$V_L = V_{in} \cdot \frac{R_2}{R_1 + R_2} = 12V \frac{8}{16 + 8} = 4V$$

$$V_R = V_{R_4} = V_{in} \frac{R_4}{R_3 + R_4} = 12V \frac{2}{3} = 8V$$

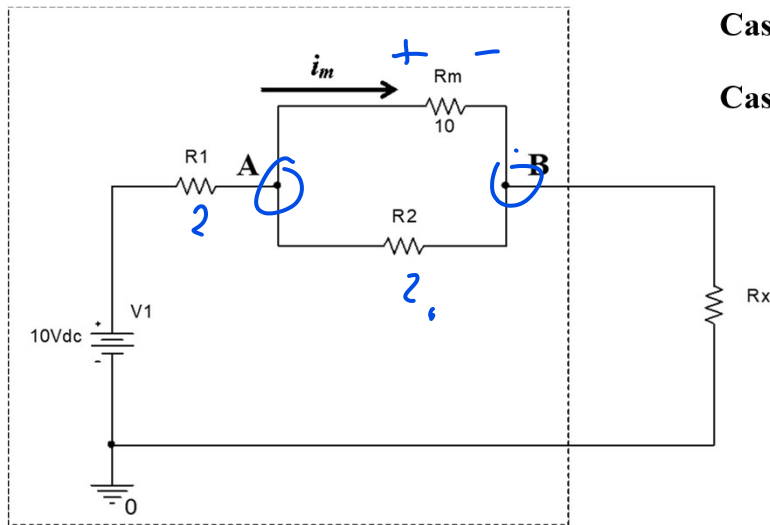
$$V_{out} = V_L - V_R = 4V - 8V = -4V$$

$$V_{R_2} = V_L - 0 = V_L$$

$$V_L = V_{in} - V_{R_1} = V_{in} - V_{in} \left( \frac{R_1}{R_1 + R_2} \right) = 12V - 8V = 4V$$

# A bit more complicated example

$$V_{AB} = V_{R_m} = R_m I_m$$



**Case 1:** Given that when  $R_x = 0 \Omega$ , the current through resistor  $R_m$  is 2 mA, i.e.  $i_m = 2 \text{ mA}$ .

**Case 2:** Given that when  $R_x = 2000 \Omega$ , the current through resistor  $R_m$  is 1 mA, i.e.  $i_m = 1 \text{ mA}$ .

Find voltage between points A and B for each of the cases described above

$$\text{case 1 : } V_{AB} = R_m i_m = 20 \text{ mV}$$

$$\text{case 2 : } V_{AB} = R_m i_m = 10 \text{ mV}$$

What is the equivalent resistance between points A and B,  $R_{AB}$ ?  
(Express in terms of  $R_2$ )

$$V_{AB} = V_{R_2} = R_2 I_2$$

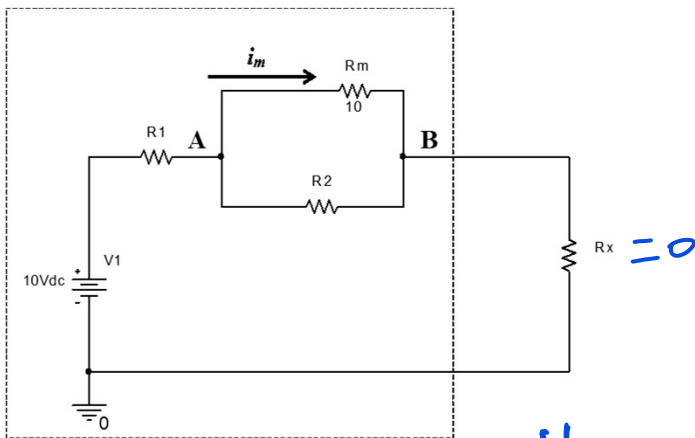
$$\boxed{R_{AB}} = R_m \parallel R_2 = \frac{R_m R_2}{R_m + R_2}$$

$R_m$  and  $R_2$  are  
in parallel

$$R_{AB} = \frac{10 R_2}{10 + R_2}$$

# A bit more complicated example (contd.)

Using voltage divider and your previous findings, develop a relationship between  $R_1$  and  $R_2$  for case 1



$$V_{AB} = 10V \cdot R_{AB}$$

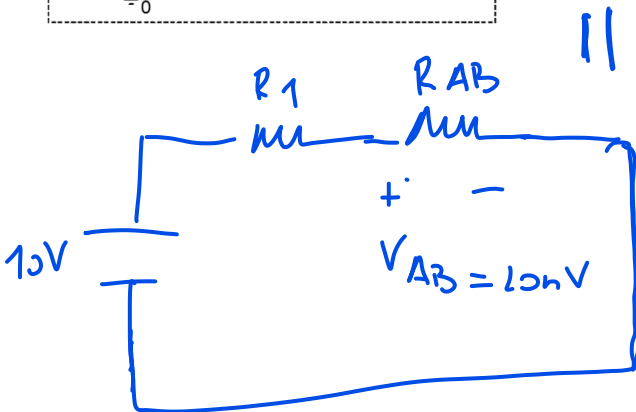
$$R_1 + R_{AB}$$

$$20mV = 10V \cdot \frac{10 R_2}{10 + R_2}$$

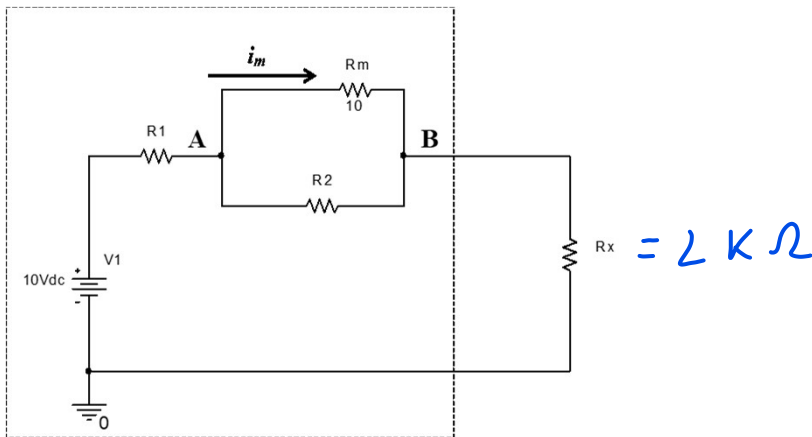
$$R_1 + \frac{10 R_2}{10 + R_2}$$

$$\Rightarrow 10R_1 - 4990R_2 + R_1R_2 = 0$$

$$R_{AB} = \frac{10 R_2}{10 + R_2}$$



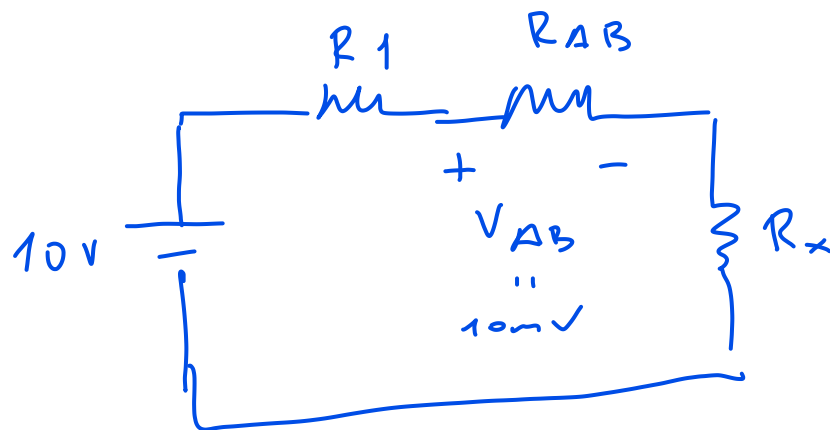
# A bit more complicated example (contd.)



Using voltage divider and your answer to parts a and b, develop a relationship between  $R_1$  and  $R_2$  for case 2

$$V_{AB} = 10V \cdot \frac{R_{AB}}{R_1 + R_{AB} + R_x}$$

$$\Rightarrow 10R_1 - 7990R_2 + R_1R_2 = -20000$$



$$R_{AB} = \frac{R_2 \cdot 10}{R_1 + 10}$$

## A bit more complicated example (contd.)

- Solve the linear relationships derived previously, to determine the values of resistors  $R_1$  and  $R_2$  such that both case 1 and 2 are satisfied

$$\underline{\text{Case 1}}: 10R_1 - 4990R_2 + R_1R_2 = 0$$

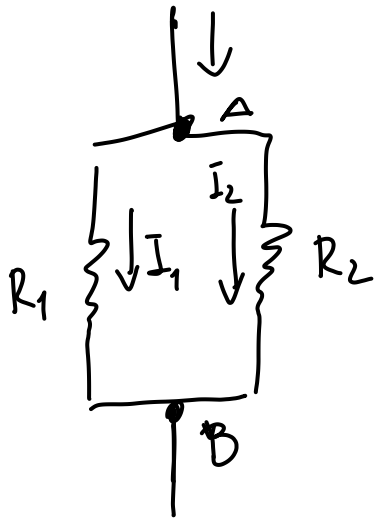
$$\underline{\text{Case 2}}: 10R_1 - 7990R_2 + R_1R_2 = -20000$$

$$\cancel{10R_1} - 4990R_2 + \cancel{R_1R_2} - (\cancel{10R_1} - 7990R_2 + \cancel{R_1R_2}) = 0 - (-20000)$$

$$3000R_2 = 20000 \Rightarrow R_2 = 6.667 \Omega$$

$$\Rightarrow R_1 = 1996 \Omega$$

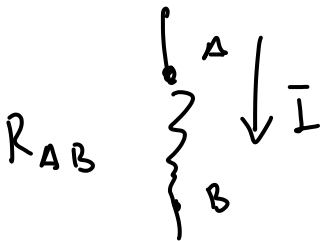
# What about Current Division?



$$I = I_1 + I_2$$

$$I_1 = \frac{V_{AB}}{R_1} \quad , \quad I_2 = \frac{V_{AB}}{R_2}$$

$$R_{AB} = R_2 \parallel R_1 = \frac{R_2 R_1}{R_1 + R_2}$$



$$V_{AB} = R_{AB} I$$

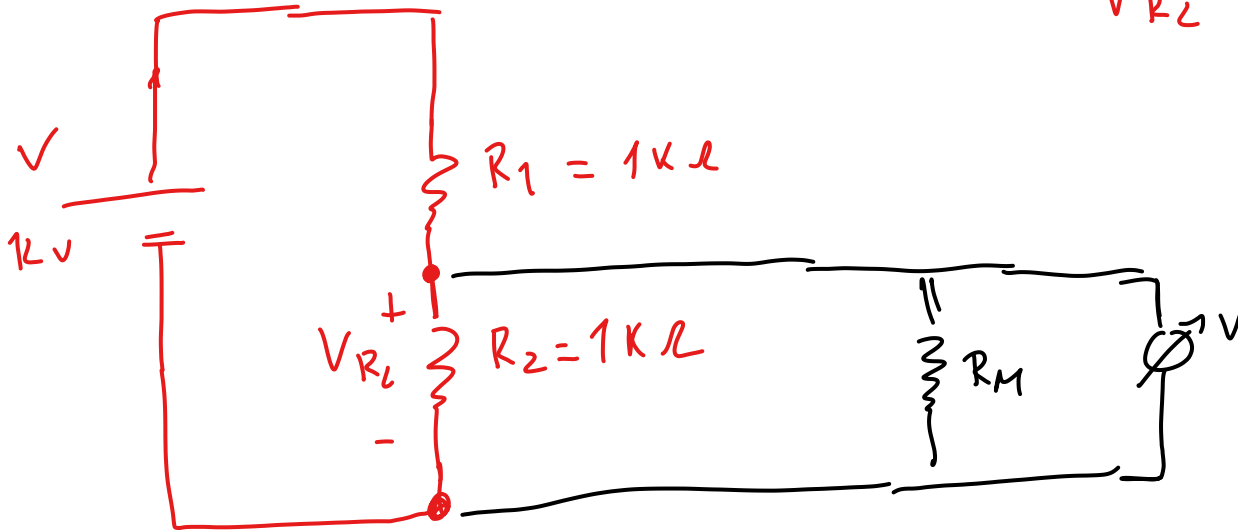
$$I_1 = \frac{R_{AB} I}{R_1} = \frac{R_2 R_1}{R_1 + R_2} \frac{1}{R_1} I = \frac{R_2}{R_1 + R_2} I$$

$$I_2 = \frac{R_1}{R_1 + R_2} I$$

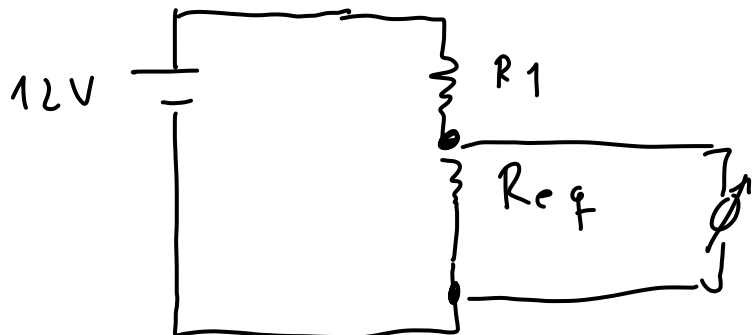


# Input Impedance of Voltmeter

$$V_{R_2} = \frac{R_2}{R_1 + R_2} V = \frac{V}{2} = 6V$$



||



$$R_{eq} = R_2 || R_M = \frac{R_2 R_M}{R_2 + R_M}$$

$$R_M \gg R_2 \rightarrow R_2$$

$$v = \frac{R_{eq}}{R_1 + R_{eq}} 12V$$

## Activity 3: Voltage Divider

- Go to the class website
- Look under class 3
- Find activity 3
- Do the activity
  - Individual submission for activity 3
  - Encouraged to discuss with others in the class on WebEx Teams
- Answer the activity using template (attached class 3)
- When complete – upload to Gradescope
  - Due Thursday, January 27<sup>th</sup> at 11:59 pm
  - Use guides to learn how to upload documents